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Integrated II UAE Edition Grade 10 Student Edition


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| Quention* <br> -سالـ |  | Leaming Outcome/Performance Criteria** | Reference(t) in the Stustent Book (Englibl Version) |  |
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|  |  |  |  |  |
| $\begin{aligned} & 5 \\ & 3 \\ & 3 \\ & 3 \\ & \frac{3}{2} \\ & \frac{1}{2} \end{aligned}$ | 1 |  | Multiply a polynomial by a monomial | 1 to 16 | 641 |
|  |  |  |  |  |
|  | 2 | Multiply binomials by using the Distributive Property and the Foil Method | 18 to 59 | 650,651 |
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|  | 3 | Find squares of sums and differences | 1 to 10 | 657 |
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|  | 4 | Fsator polynomisls by using the Distributive Property. | 1 to 10 | 665 |
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|  | 5 | Factorize binomials that are the difference of squares | 1 to 14 | 679 |
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|  | 6 | Know the precise definition of circle and find the circumferences of circles. | 1 to 15 | 227 |
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|  | 8 | Describe relationships between inscribed angles, and use those relationships to solve problems | 1 to 12 | 251 |
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|  | 9 | Identity relationships in inscribed polygons, and use those relationships to solve problems | 13 to 25 | 252 |
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|  | 10 | Solve problems involving circumscribed polygons | 19 to 26 | 260 |


$\square$

## Example 1

Simplify each expression.

1. $b\left(b^{2}-12 b+1\right)$
2. $f\left(f^{2}+2 f+25\right)$
3. $-3 m^{3}\left(2 m^{3}-12 m^{2}+2 m+25\right)$
4. $2 j^{2}\left(5 j^{3}-15 j^{2}+2 j+2\right)$
5. $2 p r^{2}\left(2 p r+5 p^{2} r-15 p\right)$
6. $4 t^{3} u\left(2 t^{2} u^{2}-10 t u^{4}+2\right)$

## Example 2

## Simplify each expression.

$$
\text { 7. }-3\left(5 x^{2}+2 x+9\right)+x(2 x-3) \quad \text { 8. } a\left(-8 a^{2}+2 a+4\right)+3\left(6 a^{2}-4\right)
$$

9. $-4 d\left(5 d^{2}-12\right)+7(d+5)$
10. $2 j\left(7 j^{2} k^{2}+j k^{2}+5 k\right)-9 k\left(-2 j^{2} k^{2}+2 k^{2}+3 j\right)$
11. $4 n\left(2 n^{3} p^{2}-3 n p^{2}+5 n\right)+4 p\left(6 n^{2} p-2 n p^{2}+3 p\right)$

## Example 3

13. NUMBER THEORY The sum of the first $n$ whole numbers is given by the expression $\frac{1}{2}\left(n^{2}+n\right)$. Expand the equation by multiplying, then find the sum of the first 12 whole numbers.
14. COLLEGE Troy's grandfather gave him $\$ 700$ to start his college savings account. Troy's grandfather also gives him $\$ 40$ each month to add to the account. Troy's mother gives him $\$ 50$ each month, but has been doing so for 4 fewer months than Troy's grandfather. Write a simplified expression for the amount of money Troy has received from his grandfather and mother after $m$ months.
15. MARKET Sophia went to the farmers' market to purchase some vegetables. She
bought peppers and potatoes. The peppers were $\$ 0.39$ each and the potatoes were $\$ 0.29$ each. She spent $\$ 3.88$ on vegetables, and bought 4 more potatoes than peppers. If $x=$ the number of peppers, write and solve an equation to find out how many of each vegetable Sophia bought.
16. GEOMETRY The volume of a pyramid can be found by multiplying the area of its base $B$ by one-third of its height. The area of the rectangular base of a pyramid is given by the polynomial equation $B=x^{2}-4 x-12$.
a. Write a polynomial equation to represent the volume of the pyramid $V$ if its height is 10 meters.

b. Find the volume of the pyramid if $x=12 \mathrm{~m}$.
$\square$

## Example $5 \quad$ Find each product.

18. $(2 y-11)\left(y^{2}-3 y+2\right)$
19. $(4 a+7)\left(9 a^{2}+2 a-7\right)$
20. $\left(m^{2}-5 m+4\right)\left(m^{2}+7 m-3\right)$
21. $\left(x^{2}+5 x-1\right)\left(5 x^{2}-6 x+1\right)$
22. $\left(3 b^{3}-4 b-7\right)\left(2 b^{2}-b-9\right)$
23. $\left(6 z^{2}-5 z-2\right)\left(3 z^{3}-2 z-4\right)$
24. $(n-5)(n+1)$
25. $(3 c+1)(c-2)$
26. $(2 x-6)(x+3)$

## Simplify.

48. $(m+2)\left[\left(m^{2}+3 m-6\right)+\left(m^{2}-2 m+4\right)\right]$
49. $\left[\left(t^{2}+3 t-8\right)-\left(t^{2}-2 t+6\right)\right](t-4)$

## Find each product.

50. $(a-2 b)^{2}$
51. $(3 c+4 d)^{2}$
52. $(x-5 y)^{2}$
53. $(2 r-3 t)^{3}$
54. $(5 g+2 h)^{3}$
55. $(4 y+3 z)(4 y-3 z)^{2}$
56. PRECISION Write each expression as a simplified polynomial.
a. $(3 c-2)\left(4 c^{2}-c^{3}+3\right)$
b. $(5 x-y)\left(3 x^{2}-2 x y\right)+(2 x+y)\left(y^{2}-4 x^{2}\right)$
c. $-2 x\left(3-x^{2}\right)(2 x+4)$
d. $(z-1)(2-z)(z+1)$
57. ART The museum where Julia works plans to have a large wall mural painted in its lobby. First, Julia wants to paint a large frame around where the mural will be. She only has enough paint for the frame to cover 100 square feet of wall surface. The mural's length will be 5 feet longer than its width, and the frame will be 2 feet wide on all sides.
a. Write an expression for the area of the mural.

b. Write an expression for the area of the frame.
c. Write and solve an equation to find how large the mural can be.
58. STRUCTURE The dimensions of the composite figure shown are given in terms of the triangle's height, $h$.
a. Write and simplify a quadratic expression for the area of the figure.

b. If $h=1.42$ units, what is the area of the figure? Round to the nearest hundredth, if necessary.
59. STRUCTURE Consider the expression $x^{4 p+1}\left(x^{1}-2 p\right)^{2 p+3}$.
a. Use the laws of exponents to simplify the expression.
b. Find any integer values of $p$ that make this expression equal to 1 for all values of $x$.


Examples 1 and 3
Find each product.

1. $(a+10)(a+10)$
2. $(b-6)(b-6)$
3. $(h+7)^{2}$
4. $(x+6)^{2}$
5. $(8-m)^{2}$
6. $(9-2 y)^{2}$
7. $(2 b+3)^{2}$
8. $(5 t-2)^{2}$
9. $(8 h-4 n)^{2}$
10. $(4 m-5 n)^{2}$


## Example 1 Use the Distributive Property to factor each polynomial.

4. $5 z^{2}+10 z$
5. $4 a^{2} b^{2}+2 a^{2} b-10 a b^{2}$
6. $5 c^{2} v-15 c^{2} v^{2}+5 c^{2} v^{3}$

## Example 2

7. PHYSICS The distance $d$ an object falls after $t$ seconds is given by $d=16 t^{2}$
(ignoring air resistance). To find the height of an object launched upward from ground level at a rate of 32 feet per second, use the expression $32 t-16 t^{2}$, where $t$ is the time in seconds. Factor the expression.
8. SWIMMING POOL The area of a rectangular swimming pool is given by the expression $12 w-w^{2}$, where $w$ is the width of one side. Factor the expression.
9. VERTICAL JUMP Your vertical jump height is measured by subtracting your standing reach height from the height of the highest point you can reach by jumping without taking a running start. Typically, NBA players have vertical jump heights of up to 34 inches. If an NBA player jumps this high, his height in inches above his standing reach height after $t$ seconds can be modeled by the expression $162 t-192 t^{2}$. Factor the expression.
10. PETS Conner is playing with his dog. He tosses a treat upward with an initial velocity of 13.7 meters per second. His hand starts at the same height as the dog's mouth, so the height of the treat above the dog's mouth in meters after seconds is given by the expression $13.7 t-4.9 t^{2}$. Factor the expression.


## Examples 1 and 2

1. $q^{2}-121$
2. $r^{4}-k^{4}$
3. $w^{4}-625$
4. $r^{2}-9 t^{2}$
5. $h^{4}-256$
6. $2 x^{3}-x^{2}-162 x+81$
7. $x^{2}-4 y^{2}$
8. $3 c^{3}+2 c^{2}-147 c-98$


## Example 1 For Exercises 1-3, refer to the circle at the right.

1. Name the circle.
2. Name the radii of the circle.
3. Name the chords of the circle.


## For Exercises 4-8, refer to the circle at the right.

4. Name the circle.
5. Name the radii of the circle.
6. Name the chords of the circle.
7. Name a diameter of the circle.

8. Name a radius not drawn as part of a diameter.

## For Exercises 9-11, refer to $\odot R$.

9. If $A B=18$ millimeters, find $A R$.
10. If $R Y=10$ inches, find $A R$ and $A B$.
11. Is $\overline{A B} \cong \overline{X Y}$ ? Explain.


## For Exercises 12-14, refer to $\odot$ L.

12. Suppose the radius of the circle is 3.5 yards. Find the diameter.
13. If $R T=19$ meters, find $L W$.
14. If $L T=4.2$ inches, what is the diameter of $\odot L$ ?


## Example 3

15. TIRES A bicycle has tires with a diameter of 26 inches. Find the radius and circumference of each tire. Round your answer to the nearest hundredth, if necessary.


## Example 5

Use $\odot D$ to find the length of each arc to the nearest hundredth. $\overline{N L}$ is a diameter.
20. $\overparen{L M}$ if the radius is 5 inches
21. $\overparen{M N}$ if the diameter is 3 yards

22. $\widehat{K L}$ if $J D=7$ centimeters
23. $N J K$ if $N L=12$ feet

## 24. $\widehat{K L M}$ if $D M=9$ millimeters

25. $\overparen{J R}$ if $K D=15$ inches

## Example 6

Write each degree measure in radians as a multiple of $\pi$.
26. $120^{\circ}$
27. $45^{\circ}$
28. $30^{\circ}$
29. $90^{\circ}$
30. $180^{\circ}$
31. $225^{\circ}$

## Example 7

## Write each radian measure in degrees.

32. $\frac{3 \pi}{4}$ radians
33. $\frac{3 \pi}{2}$ radians
34. $\frac{\pi}{3}$ radians
35. $\frac{5 \pi}{6}$ radians
36. $2 \pi$ radians
37. $\frac{\pi}{12}$ radians

## Example 8

Use $\odot Z$ to find the length of each arc to the nearest hundredth.
38. $\overparen{Q R}$, if $P Z=12$ feet
39. $\widehat{S T}$, if $S Z=8$ inches


## Example 1

## Find each measure.

1. $m \overparen{A C}$


## 2. $m \angle N$

3. $m \overparen{Q S R}$

4. $m \angle E$

5. $m \angle R$


Find each measure.
7. $m \angle N$
$(5 x+9)^{\circ}(6 y-1)^{\circ}$
$(3 y+8)^{\circ}$
9. $m \angle C$
10. $m \angle A$


## PROOF Write the specified type of proof.

11. paragraph proof

Given: $m \angle T=\frac{1}{2} m \angle S$

12. two-column proof

Given: ©C
Prove: $\triangle K M L \sim \triangle J M H$



Example 4
Find each value.

15. $x$
16. $m \angle T$

18. $m \angle J \angle K$
19. $m \angle A$
20. $m \angle C$


Example 5

## Find each measure.

23. $m \angle W$
24. $m \angle S$

25. $m \angle X$

26. USE ESTIMATION Darius bought a circular picture frame with a geometric design. The frame has a quadrilateral inscribed in a circle.
a. Estimate the value of $x$.

b. Find the exact value of $x$ and $m \angle J$.
c. Is your answer reasonable? Justify your argument.


## Example 5

19. If $m \angle B D C=12 x^{\circ}$ and $m \angle A=(4 x+4)^{\circ}$, find $m \angle A$.

20. If $m \angle Q P S=(15 x+8)^{\circ}$ and $m \angle R=(10 x-3)^{\circ}$, find $m \angle R$.


## Example 6

Each polygon is circumscribed about a circle. Find the perimeter of each polygon.
21.

22.

23.


Each polygon is circumscribed about a circle. Find the value of $x$. Then find the perimeter of each polygon.
24.

25.

26.



Examples 1, 2, 4-6
Find the area of each parallelogram, trapezoid, rhombus, or kite. Round to the nearest tenth, if necessary.
1.

3.

5. 18 mm


7.





Example 1
Find the area of each circle. Round to the nearest tenth.
1.

7 m
4. DINING Maricela is making a tablecloth for a circular table that has a diameter of 8 feet.
a. Find the area of the tabletop. Round your answer to the nearest tenth.
b. If a square yard of fabric costs $\$ 13.99$, what is the minimum Maricela will need to spend to make the tablecloth?
5. GAMES Kiyoshi is making circular tiles to display houses for his role-playing game. Each tile has a radius of 2 inches and is being made out of balsa wood that costs $\$ 1.99$ per square foot.
a. Find the area of a single tile. Round your answer to the nearest tenth.
b. How much will it cost Kiyoshi to make 30 tiles?
6. PORTHOLES A circular window on a ship is designed with a radius of 8 inches. What is the area of glass needed for the window? Round your answer to the nearest hundredth.

## Example 2

## Find the indicated measure. Round to the nearest tenth.

7. Find the diameter of a circle with an area of 94 square millimeters.
8. The area of a circle is 132.7 square centimeters. Find the diameter of the circle.
9. The area of a circle is 112 square inches. Find the radius of the circle.
10. Find the diameter of a circle with an area of 1134.1 square millimeters.
11. The area of a circle is 706.9 square inches. Find the radius of the circle.
12. Find the radius of a circle with an area of 2827.4 square feet.


## Examples 1, 2, 4, and 5

Find the lateral area and surface area of each solid. Round to the nearest tenth, if

## necessary

2. 14 m
3. 15 cm
4. 


6.


8.

10. $10 \mathrm{ft} \rightarrow \underbrace{\rightarrow}_{25 \mathrm{ft}}$
13. PAINTING Greg is painting the four walls of his bedroom and the ceiling.
a. If the height of the walls is $x$ and the edge length of the square ceiling is $2 x$, approximate the surface area Greg will be painting in terms of $x$.
14. MANUFACTURING A food distribution manufacturer is developing a new cylindrical package with a cardboard bottom and sides and a plastic lid. They are evaluating the cost of manufacturing based on the amount of cardboard used.
a. If the radius of the package is $x$ and the height is $x+4$, approximate the surface area of the package that will be cardboard in terms of $x$ and $\pi$.
b. Approximate the surface area that will be painted to the nearest tenth if $x=8$ feet.
b. Approximate the surface area of the package that will be cardboard to the nearest tenth if $x=6$ centimeters.
15. CAMPING A company that manufactures camping gear is designing a new tent shaped like a square pyramid with sidewalls made of a waterproof material.
a. If the base of the tent is $x$ units long and the slant height of the walls is
$1.5 x$ units, approximate the surface area of the sidewalls in terms of $x$.
16. TOPIARY Davea is planning to prune her landscaping bushes into toplaries shaped like cones.
a. The radius of a bush is $\frac{1}{2} x$ units and the slant height is $4 x$ units. Approximate the lateral area of one topiary in terms of $x$ and $\pi$.
b. Approximate the amount of material needed to manufacture the sidewalls if $x=9$ feet.
b. A frost is expected, and Davea is making plastic slipcovers to protect her new topiaries. Approximate the surface area of one slipcover to the nearest tenth if the slipcover does not cover the base of the topiary and $x=0.75$ meter.

Example 1
Describe each plane of symmetry for each solid.

2.

3.


## Example 2

Identify the shape of each cross section.

7.



Determine whether the circles in the figures below appear to be congruent, concentric, or neither.


## For each circle, find the exact circumference in terms of $\pi$.

36. 


37.

38.


40.

41.


## 42. PROOF Write a paragraph proof to prove Theorem 5.1.

 Given: $\odot D$ and $\odot E$Prove: $\odot D \sim \odot E$

43. USE A SOURCE Go online to research a famous clock face. Then use the
diameter of the clock face to find the circumference. Round your answer to the nearest hundredth.
44. WHEELS Zack is designing wheels for a concept car. The diameter of the wheel is 18 inches. Zack wants to make spokes in the wheel that run from the center of the wheel to the rim. In other words, each spoke is a radius of the wheel. How long are these spokes?
45. PRECISION Kathy slices through a circular cake. The cake has a diameter of 14 inches. The slice that Kathy made is straight and has a length of 11 inches. Did Kathy cut along a radius, a diameter, or a chord of the circle?

# 46. REASONING Three identical circular coins are lined up in a row as 

 shown. The distance between the centers of the first and third coins is 3.2 centimeters. What is the radius of one of these coins?47. EXERCISE HOOPS Taiga wants to make a circular hoop that he can twirl around his body for exercise. He will use a tube that is 2.5 meters long.
a. What will be the diameter of Taiga's exercise hoop? Round your answer to the nearest thousandth of a meter.
b. What will be the radius of Taiga's exercise hoop? Round your answer to the nearest thousandth of a meter.
48. WRITE How can we describe the relationships that exist between circles and line segments?
49. PERSEVERE The sum of the circumferences of circles $H, J$, and $K$ shown at the right is $56 \pi$ units. Find $K J$.

50. ANALYZE Is the distance from the center of a circle to a point
in the interior of a circle sometimes, always, or never less than the radius of the circle? Justify your argument.
51. CREATE Design a sequence of transformations that can be used to prove that $\odot D$ is similar to $\odot E$.



Examples 1 and 2
REGULARITY Find the value of $x$.

4.

5.

6.


7.

8. $\odot M \cong \odot P$


## 9. $\odot v \cong \odot w$



## Examples 3 and 4

## In $\odot P, P Q=13$ and $R S=24$. Find each measure.

10. $R T$
11. $P T$
12. $T Q$

13. USE A MODEL For security purposes a jewelry company prints a hidden watermark on the logo of its official documents. The watermark is a chord located 0.7 cm from the center of a circular ring that has a 2.5 cm radius. To the nearest tenth, what is the length of the chord?

## In $\odot A, E B=12, C D=8$, and $m \overparen{C D}=90^{\circ}$. Find each measure.

 Round to the nearest hundredth, if necessary13. $m \overparen{D E}$
14. $F D$
15. $A F$



## Examples 3 and 4

Find the area of each figure. Round to the nearest tenth, if necessary.
8.

9.

10. $4 \sqrt{3} \mathrm{in}$

12.

13.

$\square$

## Example 1

## Determine whether each expression is a polynomial. If it is a polynomial, find the

 degree and determine whether it is a monomial, binomial, or trinomial.1. $\frac{5 y^{3}}{x^{2}}+4 x$
2. 21
3. $c^{4}-2 c^{2}+1$
4. $d+3 d^{c}$
5. $a-a^{2}$
6. $5 n^{3}+n q^{3}$

Write each polynomial in standard form. Identify the leading coefficient.
7. $5 x^{2}-2+3 x$
8. $8 y+7 y^{3}$
9. $4-3 c-5 c^{2}$
10. $-y^{3}+3 y-3 y^{2}+2$
11. $11 t+2 t^{2}-3+t^{5}$
12. $2+r-r^{3}$
13. $\frac{1}{2} x-3 x^{4}+7$
14. $-9 b^{2}+10 b-b^{6}$

