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# CH11 Rules



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## Quotient Identities

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\cot \theta = \frac{\cos \theta}{\sin \theta}$$

## Reciprocal Identities

$$\cot \theta = \frac{1}{\tan \theta}$$

$$\csc \theta = \frac{1}{\sin \theta}$$

$$\sec \theta = \frac{1}{\cos \theta}$$

## Pythagorean Identities

$$\sin^2 \theta + \cos^2 \theta = 1$$

$$\tan^2 \theta + 1 = \sec^2 \theta$$

$$1 + \cot^2 \theta = \csc^2 \theta$$

## Sum Identities Addition Formulas

$$\sin(a+b) = \sin a \cos b + \cos a \sin b$$

$$\cos(a+b) = \cos a \cos b - \sin a \sin b$$

$$\tan(a+b) = \frac{\tan a + \tan b}{1 - \tan a \tan b}$$

## Difference Identities Subtraction Formulas

$$\sin(a-b) = \sin a \cos b - \cos a \sin b$$

$$\cos(a-b) = \cos a \cos b + \sin a \sin b$$

$$\tan(a-b) = \frac{\tan a - \tan b}{1 + \tan a \tan b}$$

## Double Angle Formulas

$$\sin 2a = 2 \sin a \cos a$$

$$\cos 2a = \cos^2 a - \sin^2 a$$

$$= 2 \cos^2 a - 1$$

$$= 1 - 2 \sin^2 a$$

$$\tan 2a = \frac{2 \tan a}{1 - \tan^2 a}$$

## Co-function Identities

$$\cos\left(\frac{\pi}{2} - \theta\right) = \sin \theta$$

$$\sin\left(\frac{\pi}{2} - \theta\right) = \cos \theta$$

$$\tan\left(\frac{\pi}{2} - \theta\right) = \cot \theta$$

## Even-Odd Identities

$$\sin(-\theta) = -\sin \theta$$

$$\cos(-\theta) = \cos \theta$$

$$\tan(-\theta) = -\tan \theta$$

## Half-Angle Formulas

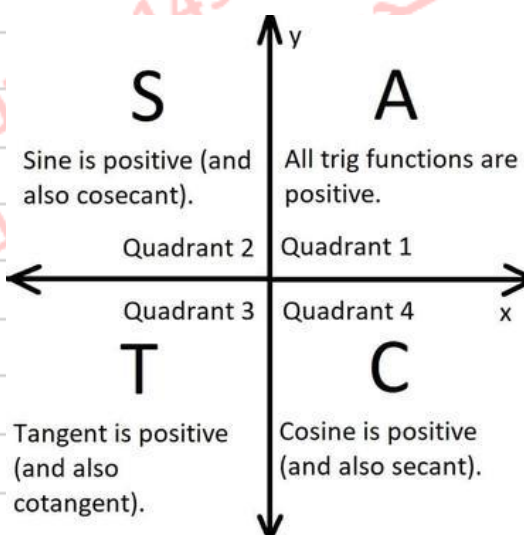
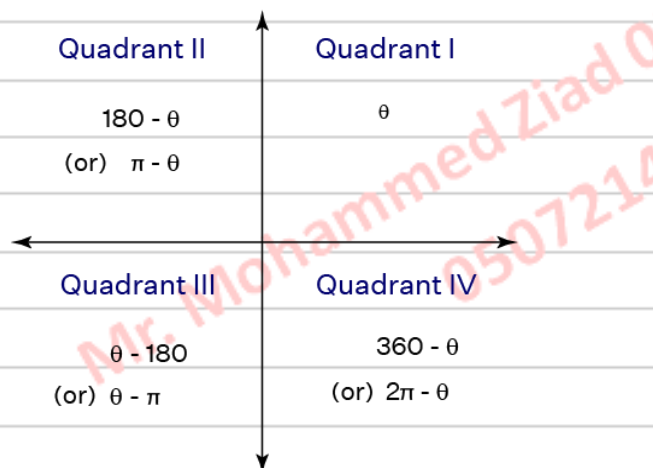
$$\sin\left(\frac{\theta}{2}\right) = \pm \sqrt{\frac{1 - \cos \theta}{2}}$$

$$\cos\left(\frac{\theta}{2}\right) = \pm \sqrt{\frac{1 + \cos \theta}{2}}$$

$$\tan\left(\frac{\theta}{2}\right) = \pm \sqrt{\frac{1 - \cos \theta}{1 + \cos \theta}}$$

## Reference Angle Formula

## Trigonometric signs:





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# CH5 Rules



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1) Let  $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ .  $A$  is invertible if and only if  $ad - cb \neq 0$ .

→  $\det(A) = |A| = \begin{vmatrix} a & b \\ c & d \end{vmatrix} = ad - cb$ .  $A^{-1} = \frac{1}{ad - cb} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$ .

2) Let  $A = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix}$ . Then  $\det(A) = |A| = a \begin{vmatrix} e & f \\ h & i \end{vmatrix} - b \begin{vmatrix} d & f \\ g & i \end{vmatrix} + c \begin{vmatrix} d & e \\ g & h \end{vmatrix}$ .

## Key Concept Cramer's Rule

3)

Let  $A$  be the coefficient matrix of a system of  $n$  linear equations in  $n$  variables given by  $AX = B$ . If  $\det(A) \neq 0$ , then the unique solution of the system is given by

$$x_1 = \frac{|A_1|}{|A|}, x_2 = \frac{|A_2|}{|A|}, x_3 = \frac{|A_3|}{|A|}, \dots, x_n = \frac{|A_n|}{|A|},$$

where  $A_i$  is obtained by replacing the  $i$ th column of  $A$  with the column of constant terms  $B$ . If  $\det(A) = 0$ , then  $AX = B$  has either no solution or infinitely many solutions.





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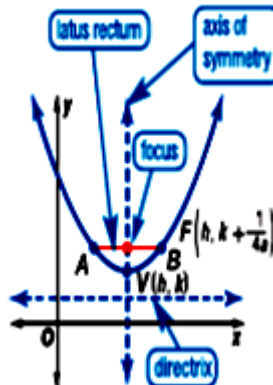
# CH6 Rules



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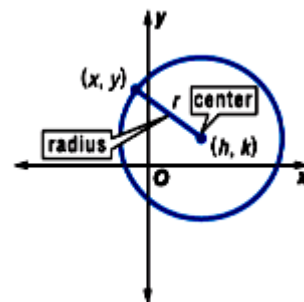
## Parabola

Equation of parabolas		
Form	$y = a(x - h)^2 + k$	$x = a(y - k)^2 + h$
Direction of opening	$a > 0$ up	$a > 0$ right
	$a < 0$ down	$a < 0$ left
Vertex	$(h, k)$	$(h, k)$
Axis of symmetry	$x = h$	$y = k$
Focus	$(h, k + \frac{1}{4a})$	$(h + \frac{1}{4a}, k)$
Directrix	$y = k - \frac{1}{4a}$	$x = h - \frac{1}{4a}$
Length of latus rectum	$ \frac{1}{a} $	$ \frac{1}{a} $



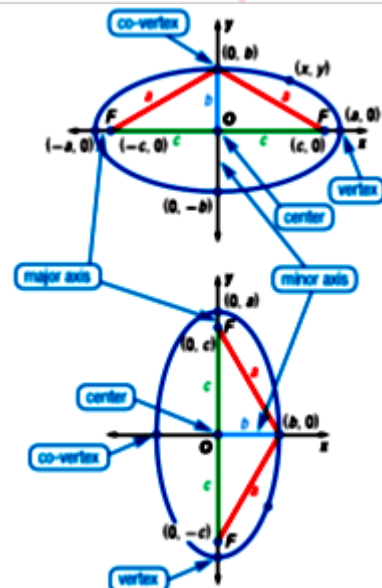
## Circle

Standard Form of Equation	$(x - h)^2 + (y - k)^2 = r^2$
Center	$(h, k)$
Radius	$r$



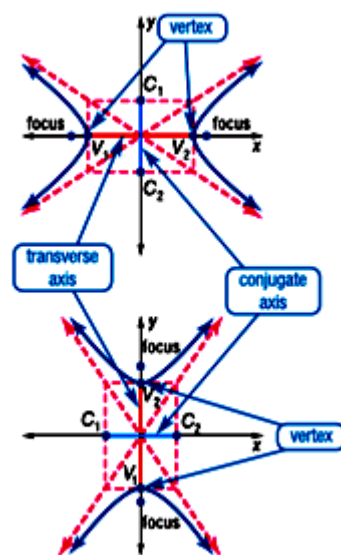
## Ellipse

Standard form	$\frac{(x - h)^2}{a^2} + \frac{(y - k)^2}{b^2} = 1$	$\frac{(y - k)^2}{a^2} + \frac{(x - h)^2}{b^2} = 1$
Orientation	Horizontal	Vertical
Vertices	$(h \mp a, k)$	$(h, k \mp a)$
Foci	$(h \mp c, k)$	$(h, k \mp c)$
Co-Vertices	$(h, k \mp b)$	$(h \mp b, k)$
Length of major axis	$2a$	$2a$
Length of minor axis	$2b$	$2b$



## Hyperbola

Standard form	$\frac{(x - h)^2}{a^2} - \frac{(y - k)^2}{b^2} = 1$	$\frac{(y - k)^2}{a^2} - \frac{(x - h)^2}{b^2} = 1$
Orientation	Horizontal	Vertical
Vertices	$(h \mp a, k)$	$(h, k \mp a)$
Foci	$(h \mp c, k)$	$(h, k \mp c)$
Co-Vertices	$(h, k \mp b)$	$(h \mp b, k)$
Length of Transverse axis	$2a$	$2a$
Length of Conjugate axis	$2b$	$2b$
Equations of asymptotes	$y - k = \mp \frac{b}{a}(x - h)$	$y - k = \mp \frac{a}{b}(x - h)$







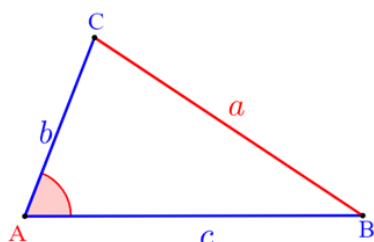
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# CH7 Rules



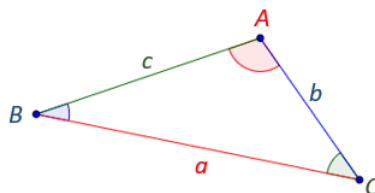
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## Cosine Rule



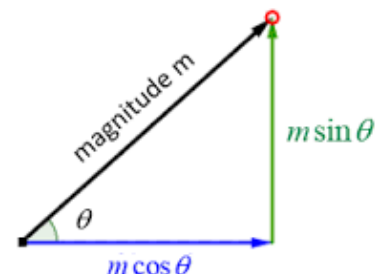
$$a^2 = b^2 + c^2 - 2bc \cos A$$

## Sine Rule or Law of Sines



$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

## Components of a Vector



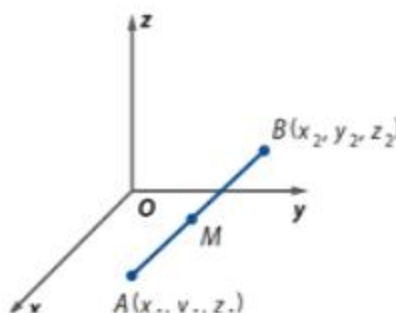
## KeyConcept Distance and Midpoint Formulas in Space

The distance between points  $A(x_1, y_1, z_1)$  and  $B(x_2, y_2, z_2)$  is given by

$$AB = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2 + (z_2 - z_1)^2}$$

The midpoint  $M$  of  $\overline{AB}$  is given by

$$M\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}, \frac{z_1 + z_2}{2}\right)$$



## KeyConcept Component Form of a Vector

The component form of a vector  $\overrightarrow{AB}$  with initial point  $A(x_1, y_1)$  and terminal point  $B(x_2, y_2)$  is given by

$$\langle x_2 - x_1, y_2 - y_1 \rangle$$

## KeyConcept Magnitude of a Vector in the Coordinate Plane

If  $\mathbf{v}$  is a vector with initial point  $(x_1, y_1)$  and terminal point  $(x_2, y_2)$ , then the magnitude of  $\mathbf{v}$  is given by

$$|\mathbf{v}| = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

If  $\mathbf{v}$  has a component form of  $\langle a, b \rangle$ , then  $|\mathbf{v}| = \sqrt{a^2 + b^2}$ .

## KeyConcept Vector Operations

If  $\mathbf{a} = \langle a_1, a_2 \rangle$  and  $\mathbf{b} = \langle b_1, b_2 \rangle$  are vectors and  $k$  is a scalar, then the following are true.

**Vector Addition**  $\mathbf{a} + \mathbf{b} = \langle a_1 + b_1, a_2 + b_2 \rangle$

**Vector Subtraction**  $\mathbf{a} - \mathbf{b} = \langle a_1 - b_1, a_2 - b_2 \rangle$

**Scalar Multiplication**  $k\mathbf{a} = \langle ka_1, ka_2 \rangle$

$$\langle a, b, c \rangle = a\mathbf{i} + b\mathbf{j} + c\mathbf{k}$$

**2 Unit Vectors** A vector that has a magnitude of 1 unit is called a **unit vector**. It is sometimes useful to describe a nonzero vector  $\mathbf{v}$  as a scalar multiple of a unit vector  $\mathbf{u}$  with the same direction as  $\mathbf{v}$ . To find  $\mathbf{u}$ , divide  $\mathbf{v}$  by its magnitude  $|\mathbf{v}|$ .

$$\mathbf{u} = \frac{\mathbf{v}}{|\mathbf{v}|} \quad \text{or} \quad \frac{1}{|\mathbf{v}|} \mathbf{v}$$



## Direction of the vector:

To find the direction of a given vector  $\langle a, b \rangle$

$$\theta = \tan^{-1}\left(\frac{b}{a}\right) \text{ if } a > 0 \quad \text{or} \quad \theta = \tan^{-1}\left(\frac{b}{a}\right) + 180^\circ, \text{ if } a < 0$$

### KeyConcept Dot Product of Vectors in a Plane

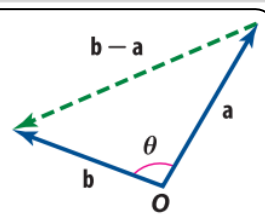
The dot product of  $\mathbf{a} = \langle a_1, a_2 \rangle$  and  $\mathbf{b} = \langle b_1, b_2 \rangle$  is defined as  $\mathbf{a} \cdot \mathbf{b} = a_1b_1 + a_2b_2$ .

### KeyConcept Orthogonal Vectors

The vectors  $\mathbf{a}$  and  $\mathbf{b}$  are orthogonal if and only if  $\mathbf{a} \cdot \mathbf{b} = 0$ .

If  $\theta$  is the angle between nonzero vectors  $\mathbf{a}$  and  $\mathbf{b}$ , then

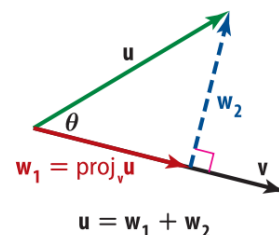
$$\cos \theta = \frac{\mathbf{a} \cdot \mathbf{b}}{|\mathbf{a}| |\mathbf{b}|}$$



### KeyConcept Projection of u onto v

Let  $\mathbf{u}$  and  $\mathbf{v}$  be nonzero vectors, and let  $\mathbf{w}_1$  and  $\mathbf{w}_2$  be vector components of  $\mathbf{u}$  such that  $\mathbf{w}_1$  is parallel to  $\mathbf{v}$  as shown. Then vector  $\mathbf{w}_1$  is called the **vector projection** of  $\mathbf{u}$  onto  $\mathbf{v}$ , denoted  $\text{proj}_v \mathbf{u}$ , and

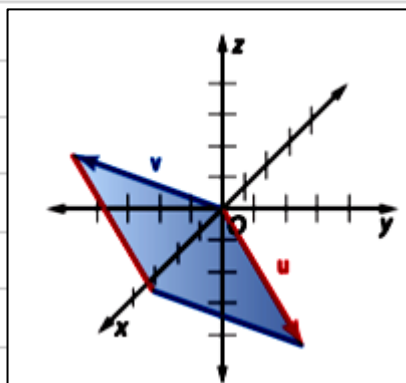
$$\text{proj}_v \mathbf{u} = \left( \frac{\mathbf{u} \cdot \mathbf{v}}{|\mathbf{v}|^2} \right) \mathbf{v}$$



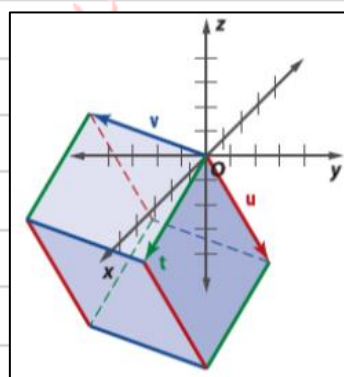
**Work:**  $W = \mathbf{F} \cdot \mathbf{d}$  , Where **f**: force , **d**: vector of displacement

**Cross product:**

$$\mathbf{a} \times \mathbf{b} = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \end{vmatrix}$$



$$\text{Area of Parallelogram} = |\mathbf{u} \times \mathbf{v}|$$



$$\text{Volume of parallelepiped} = t \cdot (\mathbf{u} \times \mathbf{v})$$